

OBTAINING ENGINEERING ESTIMATES OF AERODYNAMIC FORCES ON AIR-BREATHING SLENDER BODIES

Prabhu Ramachandran * S. C. Rajan
S. Santhakumar

Computers and Fluids Laboratory,
Department of Aerospace Engineering, IIT-Madras, Chennai 600 036

Abstract

This paper demonstrates simple techniques to obtain quick engineering estimates for the the normal load and moments on slender air-breathing shapes at small angles of attack. Rapid estimates of the normal load can be obtained using a two-dimensional, subsonic, Trefftz plane analysis. The results agree fairly well with experimental data (from NASA and AGARD) for three-dimensional slender bodies in supersonic flows. However, the method is insensitive to variations in the three-dimensional shape of the body and incapable of computing the moments on the body. The pitching moments are therefore computed using a subsonic 3D vortex panel method. These results are also in reasonably good agreement with experimental data.

1 Introduction

The present work demonstrates simple techniques using which rapid estimates of the normal load and pitching moment can be obtained. The subsonic Trefftz plane analysis is an interesting and simple technique that can be used to rapidly compute the normal load. The simplicity of the method is due to the fact that it requires just a cross-section of the body shape to compute the load. This reduces both the geometric complexity and the computational difficulties associated with a full three-dimensional analysis. The method is capable of efficiently handling air-breathing configurations. This analysis is subsonic. The justification for this is that the normal load is dependent on the vorticity distribution in the Trefftz plane. The distribution and shape of the vorticity in the Trefftz plane for highly streamlined bodies is dependent on the cross flow and not on the axial flow. Hence, for Mach numbers less than about 4, at small angles of attack, the cross flow continues to remain subsonic. Since the cross flow remains subsonic this analysis is bound to give reasonable results. This is borne out from the results presented below. The method is however incapable of predicting the moments on the body. In order to compute this a 3D vortex panel method is used. The subsonic 3D panel method is a well researched and fairly old technique but in the present work it is applied to fairly complex air-breathing geometries at supersonic Mach numbers.

The results obtained by the computations are compared with experimental data from AGARD [1] and NASA [3]. The AGARD and NASA reports provide experimental data for air-breathing slender shapes in supersonic flows.

*Ph.D. Research Scholar, prabhu@aero.iitm.ernet.in

2 Methodology

Two methods are used in the present work. A Trefftz plane analysis can be used to obtain the normal load on the body. The second method used is a 3D vortex panel method to compute the load and pitching moment on the body.

2.1 Trefftz plane analysis

It is possible to study the trailing vorticity distribution in the Trefftz plane and obtain the load on a body. The Trefftz plane is an idealized plane far downstream of the body and perpendicular to it. It contains the trailing vorticity shed by the body. Rajan and Shashidhar [8] derived an exact leading term solution for low aspect ratio wings using such an analysis. Raghavendra [7] used the same idea to obtain the load on a circular duct and a duct with fins. Govindarajan [2] used the approach to compute the normal and suction forces on an air-breathing slender body.

Given a low aspect ratio body, an axial location where the cross sectional area enclosed becomes maximum is chosen. Alternatively, the axial view of the body is projected onto the Trefftz plane and this projected two-dimensional surface is considered. The resulting two-dimensional shape is exposed to the cross flow velocity of $V_\infty \sin \alpha$. The resulting intensity of surface vorticity on the chosen cross section is computed using a linear vortex panel method using a no-penetration boundary condition. If the axial velocity of the fluid inside the body is also known, then the normal force can be computed using the Trefftz plane analysis. The details of the expressions to use and their derivations are given in [9].

The Trefftz plane analysis is insensitive to changes in the geometry so long as the maximum cross sectional shape remains unchanged. It is also incapable of computing the moments on the body. In order to compute this a 3D vortex panel method is used.

2.2 3D vortex panel method

Katz and Plotkin [4] describe two and three dimensional panel methods in considerable detail. In the present work the body is split into quadrilateral and triangular panels with vortex filaments located along the edges of the panels. The no-penetration condition is applied at the centroid of each panel. The Kutta condition is satisfied by shedding horse-shoe vortices from the trailing edge of the body. The influence matrix is solved using a Singular Value Decomposition (SVD) [6]. The SVD is used instead of the simpler and faster LU decomposition because the SVD produces more reliable results. The shapes considered in the present work have very low aspect ratios. The low aspect ratio along with the trailing edge horse-shoe vorticity tends to make the matrices involved singular. The SVD handles such singular matrices and produces good results. Once the vorticity distribution on the surface of the body is known, the force on each panel is computed using the approach detailed in Konstadinopoulos [5]. This method distributes the concentrated vorticity on each panel and then computes the pressure jump across the panel. Using this, the force distribution on the body is obtained which is then integrated to produce both the total force and the moments on the body. Hence, using the 3D vortex panel method the load and moments on the body can be obtained.

3 Results and discussion

A few air-breathing configurations are considered and the computed results are compared with experimental data. As an example we also present the results for one of the cases using the Trefftz plane analysis. For the other cases the results of the 3D vortex panel method are provided.

3.1 Comparison with AGARD data

The AGARD report[1] provides data for slender missile like shapes consisting of a solid central body with symmetrically placed axi-symmetric ducts. The cross section of the configuration is shown in Fig. 1. Exper-

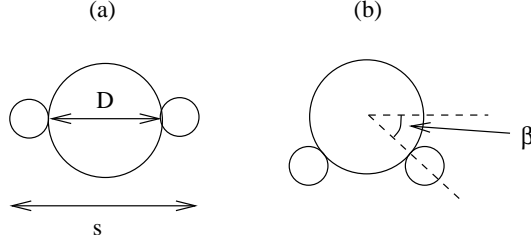


Figure 1: The various parameters used in the computation of $C_{N\alpha}$ for the missile shapes presented in the AGARD report[1].

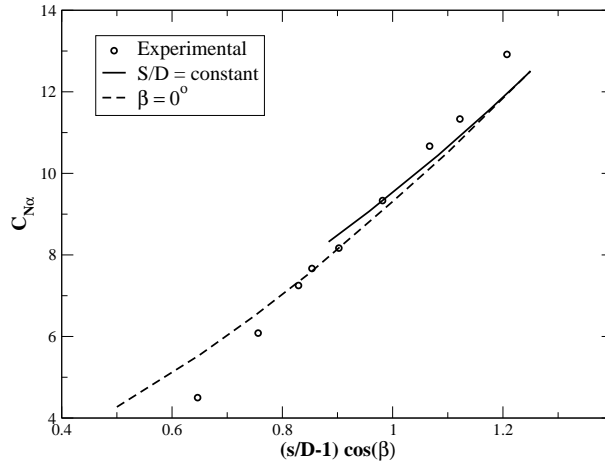


Figure 2: Computed and experimental $C_{N\alpha}$ for the AGARD configurations. The straight line plots the case when $s/D = 2.25$ and β is varied. The dashed line plots the case where $\beta = 0^\circ$ and s/D is varied. The experimental value of $M_\infty = 3.2$.

Experimental values of $C_{N\alpha}$ are provided. The Trefftz plane analysis is used to compute the load and is compared with the available experimental data. The results are plotted in Fig. 2. In one case β is held fixed at 0° and s/D is varied. In the other case β is varied between 0 and 45 degrees and s/D is held fixed. The experimental data is for the Mach number of 3.2 . Fairly good agreement is seen.

For the case where $\beta = 10^\circ$, $s/D = 2.25$, the number of panels is doubled and the convergence of the results is studied. The Grid Convergence Index (GCI)[10] for the coarse grid is computed to be 0.0071 , which indicates very good convergence.

3.2 Comparison with NASA data

The NASA experiments of Clyde Hayes [3] provide data on slender air-breathing missile configurations. The B111 configuration as per the NASA report [3] consists of two axi-symmetric air-intakes. The geometry considered for computation is shown in Fig. 3. The results of the computations using the three-dimensional panel method for C_N and C_M are plotted in Figs. 4 and 5 respectively. The results are plotted for the case where the intakes are treated as fully closed and fully open. This is done because data on the mass flow rate in the experiments was unavailable. The results are in good agreement. It is also seen that for low angles of attack the experimental results are not strongly dependent on the Mach number.

The computed trends appear correct and agree well with the experimental data. It must be mentioned that the 2D computations (Trefftz plane analysis) typically take less than a few seconds to complete for a given configuration on a Pentium 4 machine running at 1.7 GHz. The 3D panel method however takes significantly

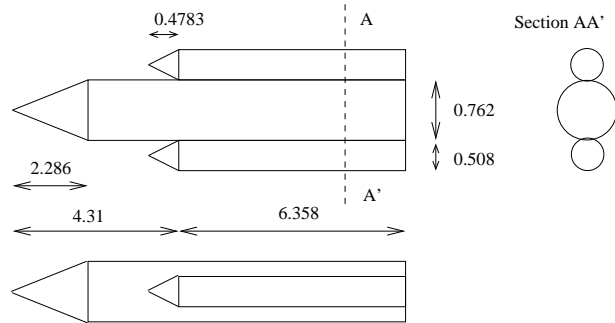


Figure 3: Cross section of the NASA B1I1 [3] configuration (all dimensions in centimeters).

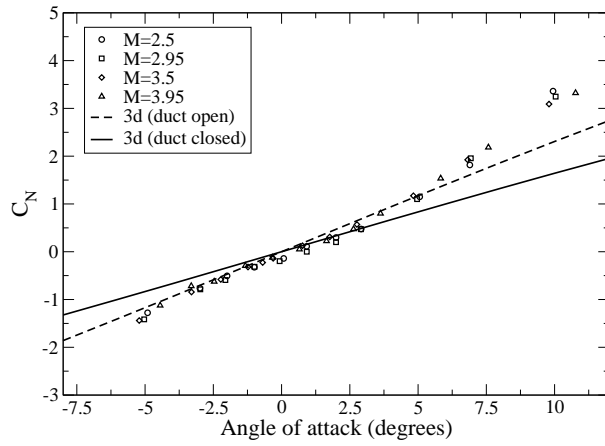


Figure 4: C_N versus angle of attack for the the NASA B1I1 configuration with the ducts placed on the side of the body as shown in Fig.3. The results are computed using the 3d vortex panel method.

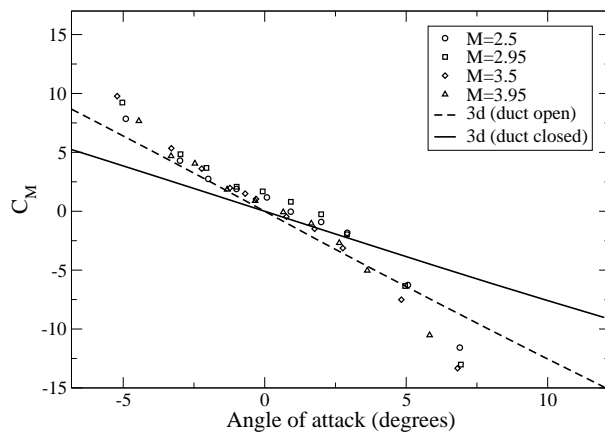


Figure 5: C_M versus angle of attack for the the NASA B1I1 configuration with the ducts placed on the side of the body as shown in Fig.3. The results are computed using the 3d vortex panel method.

more time (of the order of several minutes) due to the large number of panels and the SVD computation.

4 Conclusions

In this paper a simple technique that can be used to compute the normal load on an air-breathing slender body has been demonstrated based on the work of [9]. This technique is simple but is incapable of computing the pitching moment on the body. In order to compute this a 3D vortex panel method is used. The computed results are compared with experimental data and the agreement is found to be good. The general trends are captured and the values are reasonably close to available experimental data. It is noticed that the computations are successful in predicting the load and moment even for supersonic flows, though the computational method is purely subsonic. Since 3D panel methods are well established, these results indicate that it is certainly possible to use simple and well studied techniques to compute engineering estimates for air-breathing, low aspect ratio configurations at small angles of attack exposed to supersonic mean flow.

Acknowledgements

This work was done as part of a Defense Research and Development Laboratory (DRDL) project. The authors would like to thank DRDL, Hyderabad for their support.

References

- [1] Prediction of aerodynamic coefficients of missiles with air intakes. Technical Report CP 493, AGARD, 1990.
- [2] K. Govindarajan. Calculation of loads on air-breathing bodies. B.Tech project report, Department of Aerospace Engineering, IIT-Madras, Chennai - 600 036, May 1999.
- [3] Clyde Hayes. Aerodynamic characteristics of a series of twin-inlet air-breathing missile configurations: 1 - axisymmetric inlets at supersonic speeds. Technical Report TM 84558, NASA, Langley Research Center, Hampton, Virginia, USA, 1983.
- [4] J. Katz and A. Plotkin. *Low-Speed Aerodynamics: From Wing Theory to Panel Methods*. McGraw-Hill Education, New York, 1991.
- [5] Panagiotis Konstadinopoulos. A vortex-lattice method for general, unsteady, subsonic aerodynamics. Master's thesis, Virginia Polytechnic Institute, 1981.
- [6] William H. Press, Saul A. Teukolsky, William T. Vetterling, and Brian P. Flannery. *Numerical Recipes in 'C': The art of scientific computing*. Cambridge University Press, Cambridge, UK, 1992.
- [7] N. V. Raghavendra. Estimation of load on air-breathing bodies. B.Tech project report, Department of Aerospace Engineering, IIT-Madras, Chennai - 600 036, May 1998.
- [8] S. C. Rajan and S. Shashidhar. Exact leading term solution for low aspect ratio wings. *Journal of Aircraft*, 34(4):571–573, July–Aug. 1997.
- [9] Prabhu Ramachandran, S. C. Rajan, and S. Santhakumar. Engineering estimates of normal loads on slender air-breathing bodies. *Journal of Spacecraft and Rockets*, Under preparation.
- [10] Patrick J. Roache. *Verification and Validation in Computational Science and Engineering*. Hermosa publishers, PO Box 9110, Albuquerque, New Mexico 87119-9110 USA., 1998.