

## System Modeling, Dynamics and Control

Tutorial 6, Autumn Semester, 2006

1. A unity feedback closed-loop system consists of a proportional controller  $H(s) = K$  and the transfer function  $G(s) = (s + 2)(s^4 + 7s^3 + 15s^2 + 25s)^{-1}$  in the forward path. Find the range of values of  $K$  which yields a stable closed-loop.
2. Find the number of roots of the polynomial  $s^4 + 10s^3 + 36s^2 + 70s + 75$  that have real parts between  $-2$  and  $0$ .
3. Design a controller for the system  $G(s) = (s^2 + s + 1)^{-1}(s + 2)^{-1}$  such that the closed-loop system responds with zero steady state error to step inputs.
4. For what values of  $K$  is the closed-loop system having  $G(s) = [s^2(Ts + 1)]^{-1}$  and  $H(s) = K$  stable? Repeat in the case where derivative control ( $H(s) = Ks$ ) is used.
5. Determine the closed-loop stability of a unity feedback system having the open-loop transfer function  $G(s) = K(1 - s)/(s + 1)$ .

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